

APPENDIX A

LIST OF PUBLICATIONS

1. Alhawamda H., Taib B.M, Eshkuvatov Z.K., Ibrahim R. I, A New Class of Orthogonal Polynomials for Solving Logarithmic Singular Integral Equations, accepted for publication in International Journal of Scientific and Engineering Research (IJSER) (ISSN 2229-5518), 2018.
2. Alhawamda, H., Taib, B. M., Eshkuvatov, Z. K. and Ibrahim, R. I, Bachok-Hasham Polynomials Approach For Eigenvalues Problem of Logarithmic Singular Integral Equations, proceeding of postgraduate seminar on science and technology (KoSiST 16) eISBN:978-967-440-399-7, 2017 pp106-118.
3. Alhawamda, H., Taib, B. M., Eshkuvatov, Z. K. and Ibrahim, R. I, Bachok-Hasham Polynomials of The Second Kind For Solving A Special Class Of Singular Integral Equations, 25th National Symposium on Mathematical Sciences (SKSM25), 27-29 August 2017. (under review)
4. Alhawamda, H., Taib, B. M., Eshkuvatov, Z. K. and Ibrahim, R. I, Bachok-Hasham Polynomials of the Third and Fourth Kind For Solving A Special Class Of Singular Integral Equations, accepted for publication in International Journal of Pure and Applied Mathematics ISSN: 1311-8080, 2017.

APPENDIX B

SOME OF MATLAB CODE

Example 1

$k = 5$

$n = 5$

$a = -1$

$b = 1$

syms x

for $i = 1 : n$;

$c(i) = (\text{int}(((-2 * i . * k . ^2) / \text{pi} . ^2) ((- \text{pi} / 5) * x . ^5) . * (x . ^{k-1}) . * (1 - x . ^{2 . * k}) . ^{-0.5}) . * \text{cos}((i) . * \text{acos}(x . ^k)) , -1 , 1)) ; \text{end} ; \text{disp}(c)$

syms $xa1 = (\text{int}(((k . ^2) / ((\log(2)) . ^2 . * \text{pi} . ^2)) ((- \text{pi} / 5) * x . ^5) . * (x . ^{k-1}) . * (1 - x . ^{2 . * k}) . ^{-0.5}) . * \text{cos}((0) . * \text{acos}(x . ^k)) , -1 , 1))$

for $j = 1 : ns(j) = (x . ^{k-1}) * (1 - x . ^{2 . * k}) . ^{-0.5} . * c(j) . * (\text{cos}((j) . * \text{acos}(x . ^k))) ; \text{end} s = \text{sum}(s) ; u = a1 * (x . ^{k-1}) . * (1 - x . ^{2 . * k}) . ^{-0.5}) + s$

$f = \text{matlabFunction}(u) v = (1 / (1) . * x . ^{k-1} . * (1 - x . ^{2 . * k}) . ^{-0.5}) . * (x . ^5)$

$d = \text{matlabFunction}(v) f \text{plot}(f , [ab] , g') \text{hold on} f \text{plot}(d , [ab] , 'r') \text{hold off}$

$\text{fore} = 1 : 9 ; z1(e) = d(e / 10) - f(e / 10) \text{end} \text{fore} = 1 : 9 ; z2(e) = d(-e / 10) - f(-e / 10) \text{end} z3 = d(95 / 100) - f(95 / 100) z4 = d(-95 / 100) - f(-95 / 100)$

Example 2

$k = 3$

$n = 5$

$a = -1$

$b = 1$

syms x

for $i = 1 : n + 1 ; \text{for} j = 1 : n ; m(i , j) = \text{vpa}(\text{int}(-(\text{pi} / (j . * k)) . (\text{cos}((j) . * \text{acos}(x . ^k))) * (\text{cos}((i - 1) . * \text{acos}(x . ^k))) , -1 , 1)) ; \text{end} ; \text{end} ; \text{disp}(m)$

syms x for $i = 1 : n + 1 ; c(i) = \text{int}(\text{cos}((i - 1) . * \text{acos}(x . ^k)) , -1 , 1) ; \text{end} ; \text{disp}(c)$ syms x

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for i = 1 : n + 1; R(i) = vpa(int(((1/3) * (3 * x.^5 + pi * x.^3 * (1 - x.^6).^0.5) .* ((1 - x.^6).^(-0.5)) .*
cos((i - 1) .* acos(x.^k)), -1, 1)); end; disp(R) p = (-pi/k) .* log(2) * cI = vpa((pi/k) .*
log(2) * eye(1, n + 1))
H = I - pM = vpa([H'm(:, 1 : n)]) I1 = (pi/(2 .* k)) .* eye(n + 1) D = I1 - MD(1 : 1 : 1) =
(pi/k) .* (log(2) .* c(1) - 1) A1 = vpa(double(D)); B1 = vpa(double(R')); y1 = vpa(inv(A1) *
B1); for j = 1 : n + 1 s(j) = (x.^(k - 1) .* (1 - x.^(2 .* k))).^(-0.5) .* y1(j) .* (cos((j - 1) .*
acos(x.^k))); end s = sum(s); f = matlabFunction(s) v = x.^(k - 1) .* (1 - x.^(2 .* k)).^(-0.5) .*
(x.^3)
d = matlabFunction(v) fplot(f, [a b], 'g') hold on fplot(d, [a b], 'r') hold off

```

for e=1:9 z1(e)=d(e/10)-f(e/10) end for e=1:9 z2(e)=d(-e/10)-f(-e/10) end

Example 3 case (I)

k = 1

n = 5

a = -1

b = 1

syms x

for i = 1 : n;

for j = 1 : n;

m(i, j) = vpa(int((pi/k) .* (sin((j) .* acos(x.^k)) .* sin(acos(x.^k)).^(-1)) .*
(x.^(k - 1) .* (1 - x.^(2 .* k))).^0.5) .* (sin((i) .* acos(x.^k)) .* sin(acos(x.^k)).^(-1)), -1, 1));

end;

end;

disp(m)

syms x

for i = 1 : n; c(i) = vpa(int((1/k) .* (x.^4 + 5 .* x.^3 + 2 .* x.^2 + x - (11/8)) .* (x.^(k - 1) .*
(1 - x.^(2 .* k))).^0.5) .* sin((i) .* acos(x.^k)) .* sin(acos(x.^k)).^(-1), -1, 1)); end; disp(c)

A = vpa(double(m)); B = vpa(double(c')); y = vpa(inv(A) * B)

for j = 1 : 5 s(j) = ((1 - x.^2).^(-0.5) .* y(j) .* (cos((j) .* acos(x.^k)))); end

s = sum(s);

c = sf = matlabFunction(c) v = (1/pi) .* (1 - x.^(2 .* k)).^(-0.5) .* (x.^5 + 5 * x.^4 + (3/2) .*
x.^3 - (3/2) .* x.^2 - (5/2) .* x - (9/8)) d = matlabFunction(v)

fplot(f, [ab], 'g')

hold on fplot(d, [ab], 'r')

hold off fore = 1 : 9

z1(e) = d(e/10) - f(e/10)

end fore = 1 : 9

$$z2(e) = d(-e/10) - f(-e/10)$$

end

$$z3 = d(95/100) - f(95/100) \quad z4 = d(-95/100) - f(-95/100)$$

Example 3 case (II)

$$k = 1$$

$$n = 5$$

$$a = -1$$

$$b = 1$$

syms x for i = 1 : n;

for j = 1 : n;

$$m(i, j) = vpa(int((pi/k) .* cos((j) .* acos(x.^k))). *(x.^(k-1)). *(1-x.^(2*k)).^(-0.5)). *(cos((i) .* acos(x.^k))), -1, 1)); end; end; disp(m) syms x for i = 1 : n;$$

$$c(i) = vpa(int((-1/k) .* (x.^4 + 5 .* x.^3 + 2 .* x.^2 + x - (11/8))). *((1-x.^(2*k)).^(-0.5)). *(cos((i) .* acos(x))), -1, 1)); end;$$

$$\text{disp}(c) \quad A = vpa(\text{double}(m));$$

$$B = vpa(\text{double}(c'));$$

$$y = vpa(\text{inv}(A) * B)$$

$$\text{for } j = 1 : n \quad s(j) = vpa((1-x.^2).^(-0.5)) .* y(j) .* (\sin((j) .* acos(x.^k)) .* \sin(acos(x.^k))). (-1)); \text{end} \quad s = \text{sum}(s); \quad f = \text{matlabFunction}(s) \quad v = (-1/pi) .* (1-x.^2).^(-0.5) .* (x.^3) + (5) .* x.^2 + (5/2) .* x + (7/2))$$

$$d = \text{matlabFunction}(v)$$

$$\text{fplot}(f, [a \ b], 'g') \quad \text{hold on} \quad \text{fplot}(d, [a \ b], 'r') \quad \text{hold off} \quad \text{for } e = 1 : 9 \quad z1(e) = d(e/10) - f(e/10) \quad \text{end} \quad \text{for } e = 1 : 9 \quad z2(e) = d(-e/10) - f(-e/10) \quad \text{end} \quad m1 = d(95/100) - f(95/100) \quad m2 = d(-95/100) - f(-95/100)$$

Example 3 case (III)

$$k = 1 \quad a = -1 \quad b = 1 \quad \text{syms } x \quad b0 = @(x) (x.^(k-1)). *((1-x.^(k)).^0.5). ((1+x.^(k)).^(-0.5)). *(sin(0.5 .* acos(x.^k))). (-1) .* (sin((1-1+0.5) .* acos(x.^k))). *(x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$$

$$b1 = @(x) (x.^(k-1)). *((1-x.^(k)).^0.5). ((1+x.^(k)).^(-0.5)) .* (sin(0.5 .* acos(x.^k))). (-1) .* (sin((2-1+0.5) .* acos(x.^k))). *(x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$$

$$b2 = @(x) (x.^(k-1)). *((1-x.^(k)).^0.5). ((1+x.^(k)).^(-0.5)) .* (sin(0.5 .* acos(x.^k))). (-1) .* (sin((3-1+0.5) .* acos(x.^k))). *(x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$$

$$b3 = @(x) (x.^(k-1)). *((1-x.^(k)).^0.5). ((1+x.^(k)).^(-0.5)) .* (sin(0.5 .* acos(x.^k))). (-1) .* (sin((4-1+0.5) .* acos(x.^k))). *(x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8)); \quad b4 = @(x)$$

$$(x.^(k-1)). *((1-x.^(k)).^0.5). ((1+x.^(k)).^(-0.5)) .* (sin(0.5 .* acos(x.^k))). (-1) .* (sin((5-1+0.5) .* acos(x.^k))). *(x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8)); \quad b5 = @(x)$$

$$(x.^(k-1)). *((1-x.^(k)).^0.5). ((1+x.^(k)).^(-0.5)) .* (sin(0.5 .* acos(x.^k))). (-1) .* (sin((6-1+0.5) .* acos(x.^k))). *(x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$$

$a0 = vpa((k.^2/pi.^2). * integral(b0, -1, 1))$ $a1 = vpa((k.^2/pi.^2). * integral(b1, -1, 1))$
 $a2 = vpa((k.^2/pi.^2). * integral(b2, -1, 1))$ $a3 = vpa((k.^2/pi.^2). * integral(b3, -1, 1))$ $a4 =$
 $vpa((k.^2/pi.^2). * integral(b4, -1, 1))$ $a5 = vpa((k.^2/pi.^2). * integral(b5, -1, 1))$
 $s = a0. * ((x.(k-1). * (1-x.(k)).^(-0.5)). * (1+x.(k)).^(0.5)). * (cos(0.5. * acos(x.^k))).^(-$
 $1)). * (cos((0+0.5). * acos(x.^k))) + a1. * ((x.(k-1). * (1-x.(k)).^(-0.5)). * (1+x.(k)).^(0.5)). * ($
 $cos(0.5. * acos(x.^k))).^(-1)). * (cos((1+0.5). * acos(x.^k))) + a2. * ((x.(k-1). * (1-$
 $x.(k)).^(-0.5)). * (1+x.(k)).^(0.5)). * (cos(0.5. * acos(x.^k))).^(-1)). * (cos((2+0.5). * acos(x.^k))) +$
 $a3. * ((x.(k-1). * (1-x.(k)).^(-0.5)). * (1+x.(k)).^(0.5)). * (cos(0.5. * acos(x.^k))).^(-1)). * ($
 $cos((3+0.5). * acos(x.^k))) + a4. * ((x.(k-1). * (1-x.(k)).^(-0.5)). * (1+x.(k)).^(0.5)). * ($
 $cos(0.5. * acos(x.^k))).^(-1)). * (cos((4+0.5). * acos(x.^k))) + a5. * ((x.(k-1). * (1-$
 $x.(k)).^(-0.5)). * (1+x.(k)).^(0.5)). * (cos(0.5. * acos(x.^k))).^(-1)). * (cos((5+0.5). * acos(x.^k)))$
 $f = matlabFunction(s)$ $v = (1/pi). * x.(k-1). * (1+x.(k)).^0.5. * ((1-x.(k)).^-0.5). * (x.^4 +$
 $4 * x.^3 - (5/2). * x.^2 + x - (7/2))$ $d = matlabFunction(v)$

$fplot(f,[a b], 'g')$ hold on $fplot(d,[a b], 'r')$ hold off for $e=1:9$ $z1(e)=d(e/10)-f(e/10)$ end
for $e=1:9$ $z2(e)=d(-e/10)-f(-e/10)$ end $z3=d(95/100)-f(95/100)$ $z4=d(-95/100)-f(-95/100)$

Example 3 case (iv)

$k = 1$

$a = -1$

$b = 1$

syms x

$b0 = @(x)(x.(k-1). * ((1+x.(k)).^0.5). * ((1-x.(k)).^-0.5). * (cos(0.5. * acos(x.^k))).^(-$
 $1)). * (cos((1-1+0.5). * acos(x.^k))). * (x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$

$b1 = @(x)(x.(k-1). * ((1+x.(k)).^0.5). * ((1-x.(k)).^-0.5). * (cos(0.5. * acos(x.^k))).^(-$
 $1)). * (cos((2-1+0.5). * acos(x.^k))). * (x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$

$b2 = @(x)(x.(k-1). * ((1+x.(k)).^0.5). * ((1-x.(k)).^-0.5). * (cos(0.5. * acos(x.^k))).^(-$
 $1)). * (cos((3-1+0.5). * acos(x.^k))). * (x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$

$b3 = @(x)(x.(k-1). * ((1+x.(k)).^0.5). * ((1-x.(k)).^-0.5). * (cos(0.5. * acos(x.^k))).^(-$
 $1)). * (cos((4-1+0.5). * acos(x.^k))). * (x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$

$b4 = @(x)(x.(k-1). * ((1+x.(k)).^0.5). * ((1-x.(k)).^-0.5). * (cos(0.5. * acos(x.^k))).^(-$
 $1)). * (cos((5-1+0.5). * acos(x.^k))). * (x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$

$b5 = @(x)(x.(k-1). * ((1+x.(k)).^0.5). * ((1-x.(k)).^-0.5). * (cos(0.5. * acos(x.^k))).^(-$
 $1)). * (cos((6-1+0.5). * acos(x.^k))). * (x.^4 + 5 * x.^3 + 2 * x.^2 + x - (11/8));$

$a0 = -vpa((k.^2/pi.^2). * integral(b0, -1, 1))$ $a1 = -vpa((k.^2/pi.^2). * integral(b1, -1, 1))$ $a2 =$

$-vpa((k.^2/pi.^2). * integral(b2, -1, 1))$ $a3 = -vpa((k.^2/pi.^2). * integral(b3, -1, 1))$ $a4 =$

$-vpa((k.^2/pi.^2). * integral(b4, -1, 1))$ $a5 = -vpa((k.^2/pi.^2). * integral(b5, -1, 1))$

$s = a0. * ((x.(k-1). * (1+x.(k)).^(-0.5)). * (1-x.(k)).^(0.5)). * (sin(0.5. * acos(x.^k))).^(-$

```

1)),*(sin((0+0.5).*acos(x.^k))))+a1.*((x.^(k-1)).*(1+x.^(k)).^(-0.5)).*(1-x.^(k)).^(0.5)).*
(sin(0.5.*acos(x.^k))).^(-1)).*(sin((1+0.5).*acos(x.^k))))+a2.*((x.^(k-1)).*(1+
x.^(k)).^(-0.5)).*(1-x.^(k)).^(0.5)).*(sin(0.5.*acos(x.^k))).^(-1)).*(sin((2+0.5).*acos(x.^k))))+
a3.*((x.^(k-1)).*(1+x.^(k)).^(-0.5)).*(1-x.^(k)).^(0.5)).*(sin(0.5.*acos(x.^k))).^(-1)).*
(sin((3+0.5).*acos(x.^k))))+a4.*((x.^(k-1)).*(1+x.^(k)).^(-0.5)).*(1-x.^(k)).^(0.5)).*
(sin(0.5.*acos(x.^k))).^(-1)).*(sin((4+0.5).*acos(x.^k))))+a5.*((x.^(k-1)).*(1+
x.^(k)).^(-0.5)).*(1-x.^(k)).^(0.5)).*(sin(0.5.*acos(x.^k))).^(-1)).*(sin((5+0.5).*acos(x.^k))))
f=matlabFunction(s)v=(-1/pi).*x.^(k-1).*(1-x.^(k)).^0.5.*((1+x.^(k)).^(0.5)).*(x.^4+
6.*x.^3+(15/2).*x.^2+6.*x+(7/2))d=matlabFunction(v)

```

```

fplot(f,[a b],'g') hold on fplot(d,[a b],'r') hold off for e=1:9 z1(e)=d(e/10)-f(e/10) end
for e=1:9 z2(e)=d(-e/10)-f(-e/10) end z3=d(95/100)-f(95/100) z4=d(-95/100)-f(-95/100)

```

Example 4 case (ii)

```
k = 3
```

```
n = 5
```

```
a = -1
```

```
b = 1
```

```
syms x
```

```
for i = 1 : n;
```

```
for j = 1 : n;
```

```

m(i,j) = vpa(int((pi.^2/k.^2).*cos((j).*acos(x.^k)).*(x.^(k-1)).*(1-x.^(2.*k)).^(-0.5)).*
(cos((i).*acos(x.^k))),-1,1));end;end;disp(m) symsx for i = 1 : n;c(i) = vpa(int((pi/k).*
(cos((4).*acos(x.^k)).*(x.^(k-1)).*(1-x.^(2.*k)).^(-0.5)).*(cos((i).*acos(x.^k))),-1,1))
end;

```

```
disp(c) A = vpa(double(m));B = vpa(double(c'));s = vpa(inv(A)*B)
```

```

forj = 1 : n s(j) = (x.^2.*(1-x.^6)).^(0.5).*y(j).*sin((j).*acos(x.^k)).*sin(acos(x.^k)).^(-
1));end s = sum(s);

```

```
f = matlabFunction(s)v = (3/pi).*x.^2.*(1-x.^6)).^(0.5).*(8*x.^9-4*x.^3)
```

```
d = matlabFunction(v)fplot(f,[ab],'-k')hold on fplot(d,[ab],-'k')hold off
```

```
fore = 1 : 9z1(e) = d(e/10) - f(e/10)endfore = 1 : 9z2(e) = d(-e/10) - f(-e/10)end
```

```
f = matlabFunction(s)
```

```
v = 3 pi x^2 (1 - x^6)^(0.5) (8 x^9 - 4 x^3)
```

```
d = matlabFunction(v)
```

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